

Last time: more Newton

- Physical Laws and definitions of force, velocity, acceleration
- #1: Inertia; #2: Forces ($F=ma$); #3: Action/Reaction
- Newton's Law of Universal Gravitation
 - gravity as a central, universal, cosmic force

Today: Rocket Science

- orbits - circular velocity and escape velocity
- Holman Transfer orbit - adjust size and eccentricity to take a trip from one planet to the next
- flyby, orbit, and landing
- Gravitational assist

Rocket Science:

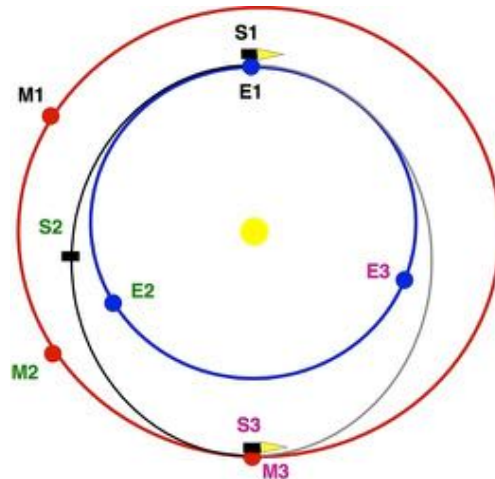
How to send a spacecraft to Mars

0- Don't shoot AT it - it is a MOVING target !!!

1. accelerate to break free from Earth's gravity

2. coast in "transfer orbit" to reach Mars' orbit

3. get captured by the gravity of Mars



Newton's Legacy

- **Force of Gravity pulls planets towards Sun**
 - without gravity, planets would fly away in straight lines
- Newton's theory of gravity explains -**simply**- the orbits of the planets

Understanding motions of the planets was the principal discovery of astronomy from prehistory through 1700.

- Improved observations ("technology") demanded more precise models of the Solar System
- This precision was
 - **approached** by complex models (epicycles, etc.) but
 - **achieved** by discovery of the underlying **simplicity: Gravity**

1- accelerate to break free of Earth

- Circular velocity

= speed needed to maintain a circular orbit

$$v_c^2 \approx \frac{\text{Mass of main body}}{\text{size of orbit}}$$

- for near-Earth orbit, $v_c = 7.7$ km/s (=17,000 mph)
- for Earth around Sun, $v_c = 30$ km/s (= 67,000 mph)
- for near-Mars orbit, $v_c = 3.4$ km/s (= 7,600 mph)
- for Mars around Sun, $v_c = 24$ km/s (= 54,000 mph)

- Escape Velocity

= speed needed to escape (forever) grav. pull

$$v_{\text{esc}} = v_c \times \sqrt{2}$$

from near-Earth orbit,

$$v_{\text{esc}} = 11 \text{ km/s} (= 24,000 \text{ mph}) \text{ away from Earth}$$

Exceed escape velocity – into a Sun-centered orbit!

2- coast in “transfer orbit” to Mars

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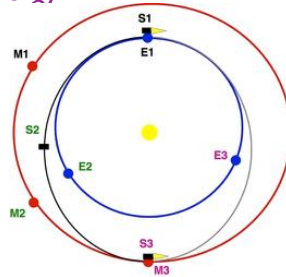
- **Transfer Orbit:** an ellipse with:

- **perihelion** at Earth distance (1 a.u.)
- **aphelion** at Mars min. distance (1.38 a.u.)
 $e=0.160$; $a=1.19\text{a.u.}$; $P = 15.6$ months
- this gets probe to Mars with **minimum energy**

Kepler 1:
perihelion distance = $a \times (1-e)$
aphelion distance = $a \times (1+e)$

How fast do you need to go to achieve the transfer orbit to Mars?

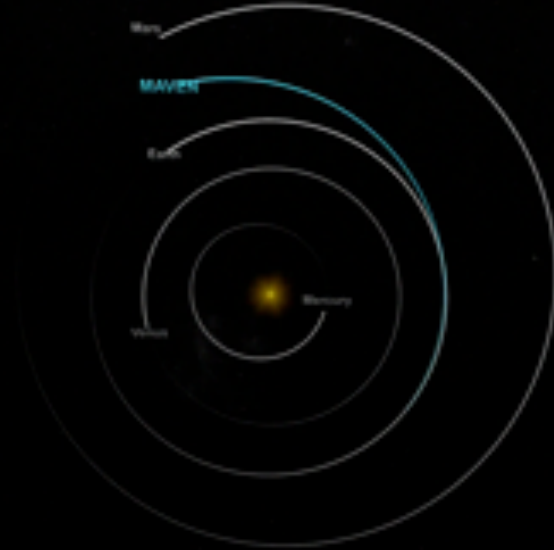
Kepler's Second Law tells us!
32.3 km/s w.r.t. the Sun



- **Coast for $P/2$ (about 7+ months):**

- If you left at the right time, reach Mars near aphelion
- "Launch Window" open every 25 months (or so)

MAVEN Cruise trajectory



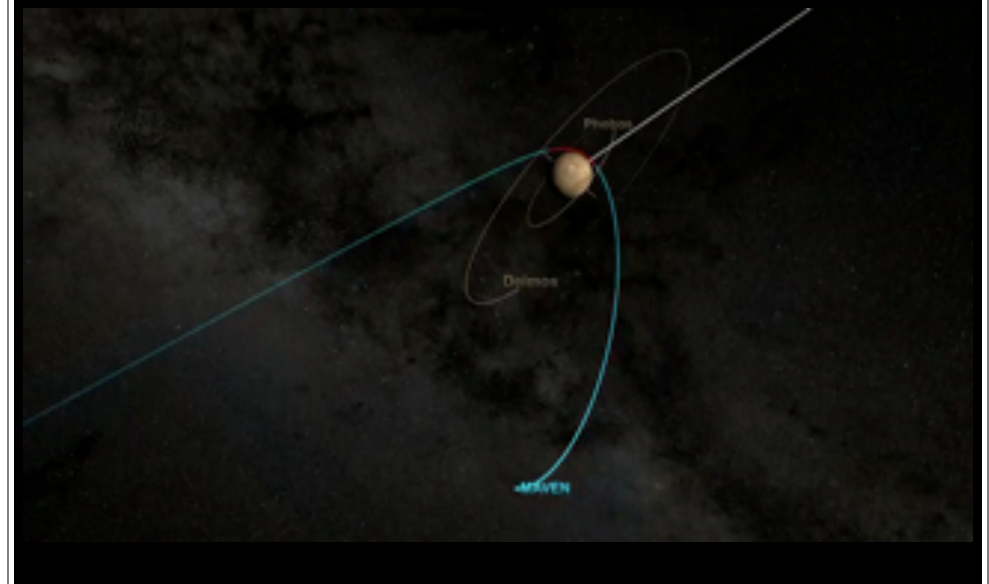
3- get captured by Mars

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- **Rendezvous with Mars:**

- spacecraft speed = 23.4 km/s (via Kepler 2)
- **Mars speed = 26.7 km/s**
- relative velocity = **3.3 km/s**
- **circular velocity for Mars orbit is 3.4 km/s**
 - an orbital maneuver (burn) is needed to reach Mars orbit
 - timing is critical here!

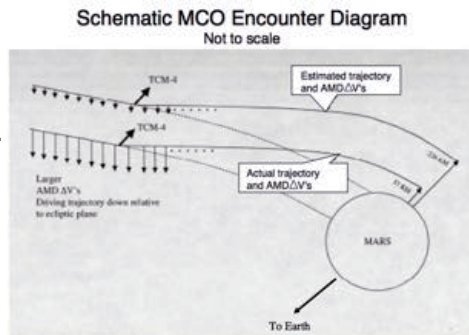
MAVEN arrival



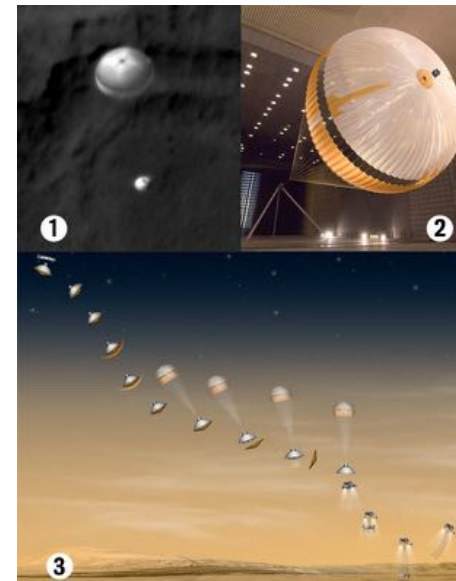
3- get captured by Mars

- Rendezvous with Mars:
 - spacecraft speed = 23.4 km/s (via Kepler 2)
 - Mars speed = 26.7 km/s
 - relative velocity = 3.3 km/s
- circular velocity for Mars orbit is 3.4 km/s
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Mars Climate Observer (1999) got it wrong...
unit confusion (English vs. Metric)
came too close - burned up in atmosphere

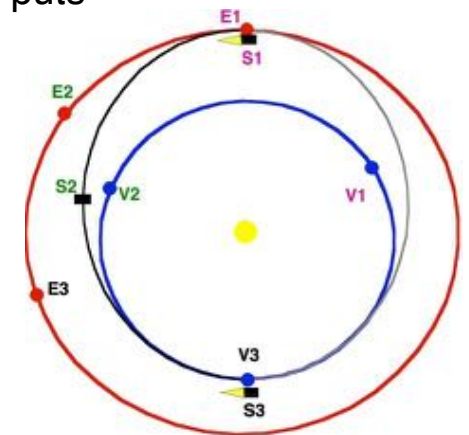


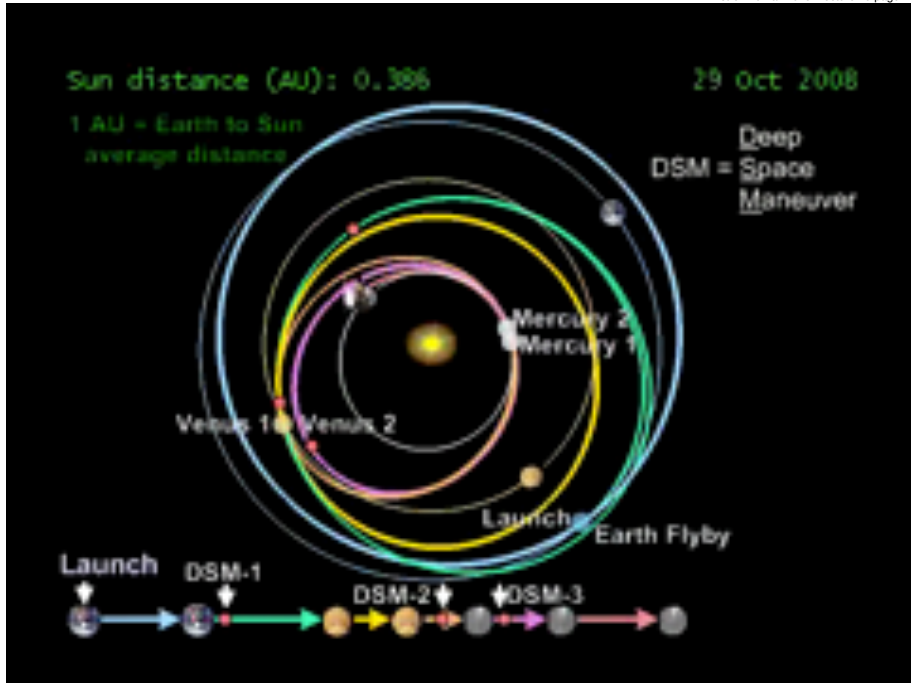
Curiosity Rover - landing



Similar scheme to reach Venus orbit

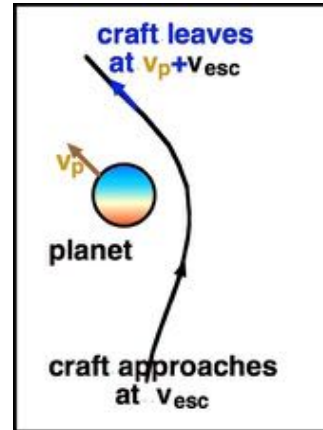
- BUT: **Decelerate** from Earth
- Venus transfer orbit puts
 - Earth at **Aphelion**
 - Venus at **Perihelion**
- **MERCURY:**
much tougher



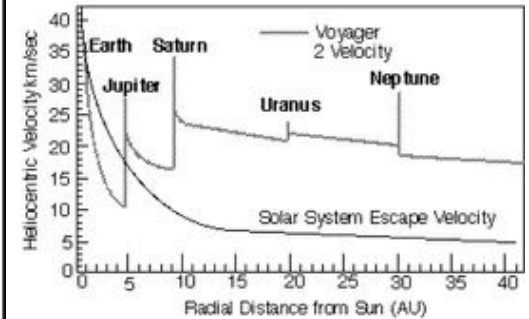


Getting to the Outer Planets

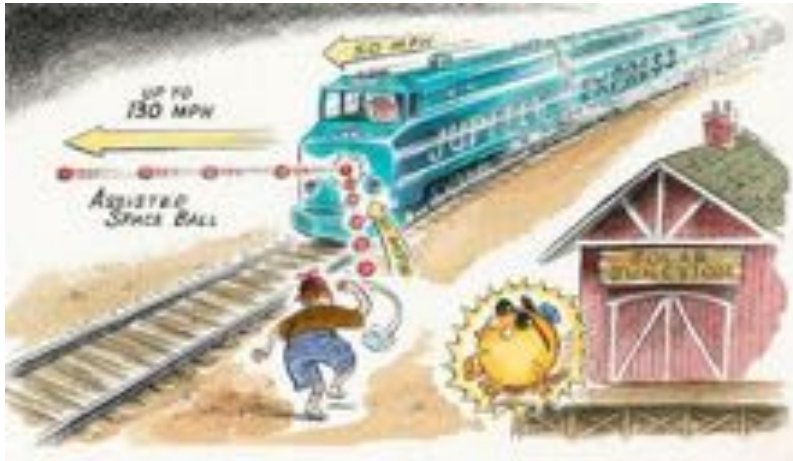
- requires a lot of energy (fuel) and time
- special trick: **gravity assist**
 - slingshot effect of planet's gravity on the spacecraft



Voyager 2 Gravity Assist Velocity Changes

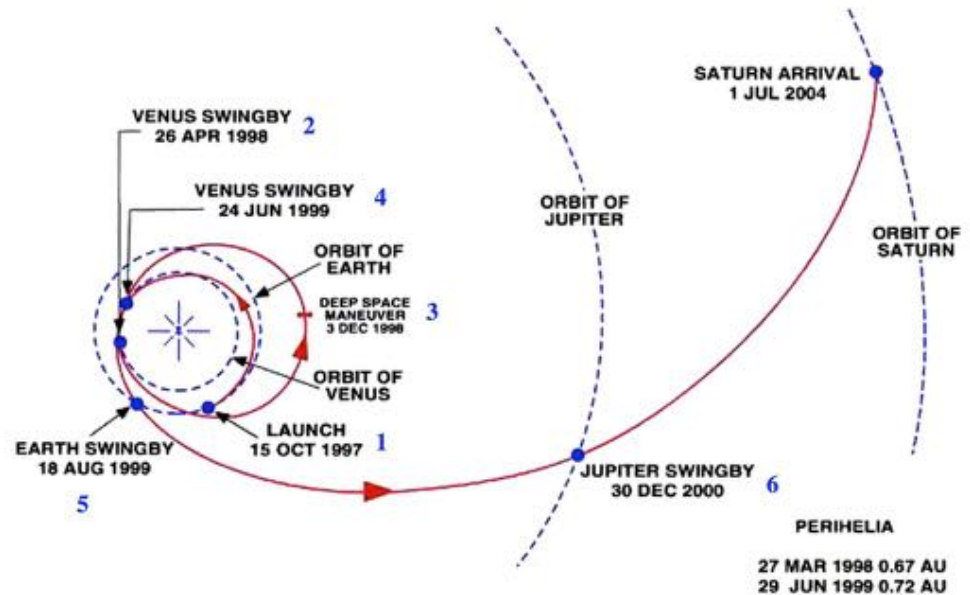


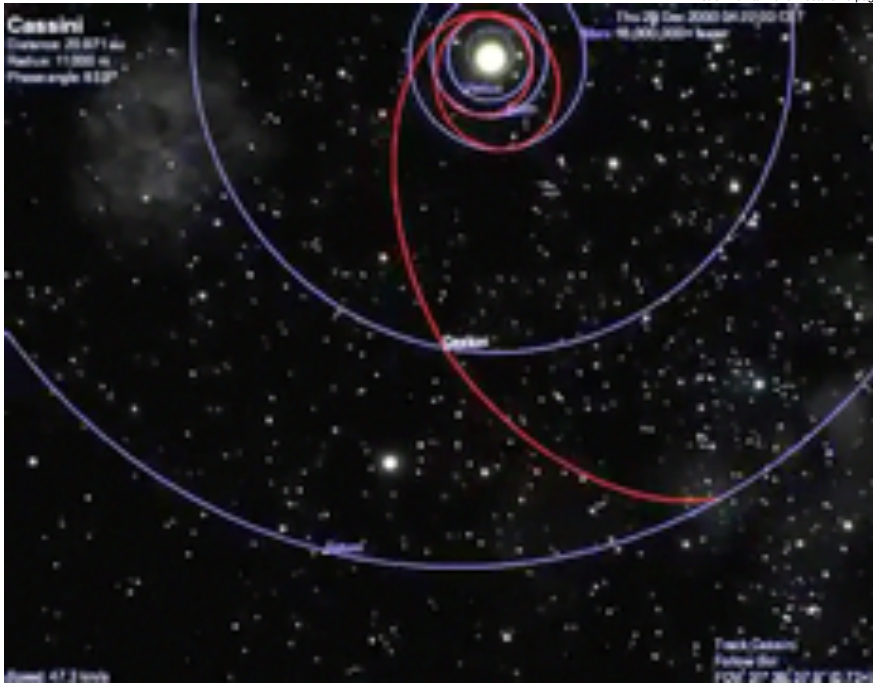
craft steals angular momentum (orbital energy) from planet



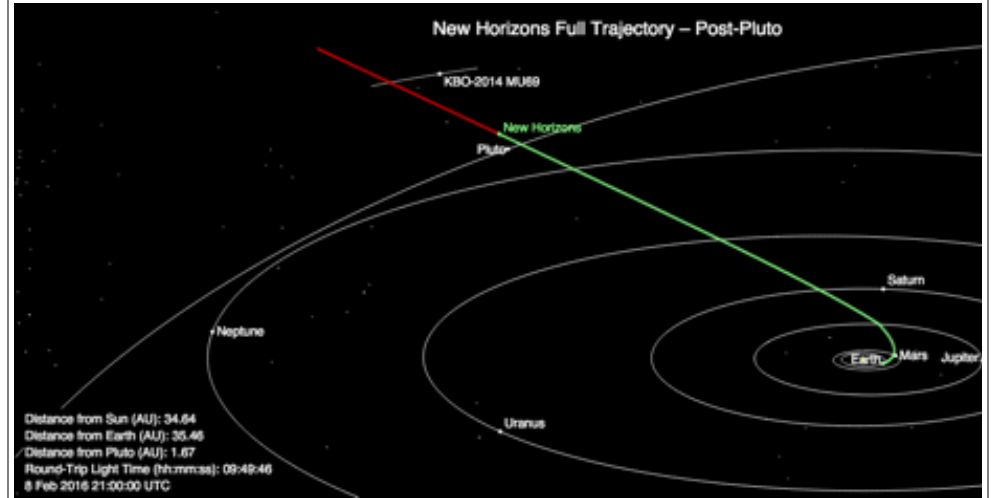
<http://www2.jpl.nasa.gov/basics/grav/primer.php>

CASSINI INTERPLANETARY TRAJECTORY

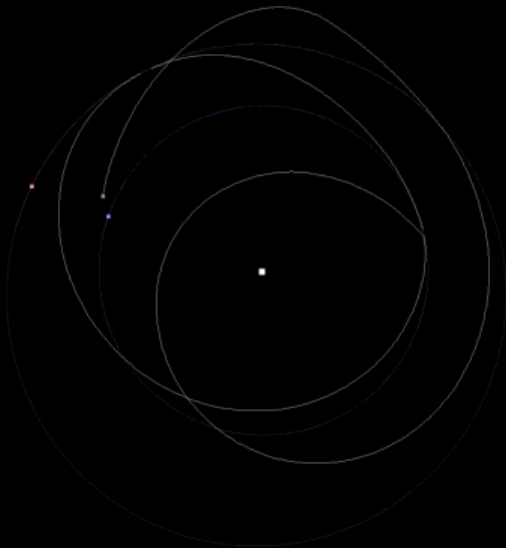




New Horizons to Pluto and beyond



Trajectories in “The Martian”



Trajectories in “The Martian”

